

## Life-Time of Vibration Insulators Made of Metal Rubber Material under Random Load

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**Abstract:** MR material (Metal Rubber) is manufactured by cold pressing of randomly placed wire spiral made of stainless steel. It has high strength, large energy dissipation coefficient, large working ability in aggressive environment, under high and low temperature. Vibration insulators with elastic-damping elements made of MR material are used widely. A research of life-time of vibration insulators made of MR material under random load is presented in this study. Dependencies of vibration insulator life-time on random load stress are obtained for different relative density, wire diameter, preliminary static deformation of MR material. Different types of MR material wearing are considered. Results of the present research are necessary for design of vibration protection systems with vibration insulators made of MR material.

**Key words:** Metal Rubber material, life-time, stress, random load, design

### INTRODUCTION

MR material (Metal Rubber) is manufactured by cold pressing of randomly placed wire spiral made of stainless steel (Ponomarev, 2014; Troynikov and Moskalev, 2014). It has high strength, large energy dissipation coefficient, large working ability in aggressive environment, under high and low temperature. Properties of this material don't change during time of its storage. Vibration insulators with elastic-damping elements made of MR material are used widely in aerospace industry, railway, cars, etc. (Ao *et al.*, 2005; Jiang *et al.*, 2008; Troynikov *et al.*, 2014; Xia *et al.*, 2009). For example, it is used for reducing of resonant stress level in gas turbine engine (Popov *et al.*, 2014). Damper made of MR material can work in combination with a hydrodynamic damper of shaft (Falaleev *et al.*, 2014).

Load on transport system is random often. Thus for design of vibration protection system with vibration insulators made of MR material it is necessary to know a life-time of these vibration insulators under random load. However, this question is not researched till the present time. Researches of life-time of vibration insulators made of MR material for harmonic vibration load exist only (Ao *et al.*, 2006; Ulanov and Ponomarev, 2008; Yan *et al.*, 2013). These researches consider MR as anisotropic quasi-continuous media and use for calculation of its life-time the same parameters as for usual structure materials: fatigue limits for normal and tangential stress  $\sigma_{-1}$  and  $\tau_{-1}$ , respectively (Ao *et al.*, 2006; Timoshenko and Goodier, 1951). Consideration of MR as anisotropic

quasi-continuous media is used for its calculation by finite element method (Ulanov and Ponomarev, 2009; Ulanov, 2014) and gives good results. Thus, it is possible to apply this approach for research of life-time of MR material under random load.

### RESEARCH

For research of life-time of MR vibration isolators under random load sleeve-type vibration isolator (Fig. 1) were used. An outer diameter of sleeves is  $D_1 = 16$  mm, inner diameter is  $D_2 = 6.5$  mm, height of sleeves in free condition was from  $H = 4.7$  mm till 5.3 mm, height of sleeves into vibration isolator is  $H_1 = 4.4$  mm.

Direction of load was in direction of pressing during MR material manufacturing. This direction is more usual

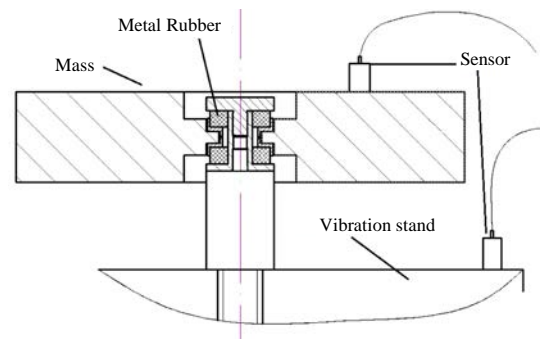


Fig. 1: Loading of sleeve-type vibration isolator for life-time test in direction of MR material pressing



Fig. 2: Sleeves of different wire diameter after wearing; Left:  $d_w = 0.2$  mm; middle:  $d_w = 0.15$  mm and right:  $d_w = 0.1$  mm

for MR vibration isolator work. Frequency range of random load changed from [5...200] to [5...2000] Hz. Parameters of MR material depend on its relative density:

$$\bar{\rho} = \frac{\rho_{MR}}{\rho_s}$$

Here:

$\rho_{MR}$  = density of MR material

$\rho_s$  = density of steel

wire diameter  $d_w$  and preliminary static relative deformation is  $\epsilon_Q = Q/H$  (here,  $Q = H - H_1$  is absolute static deformation). Ranges of researched parameters of MR material were:  $\bar{\rho} \in [0.2...0.28]$ ,  $d_w \in [0.1...0.2]$  mm,  $\epsilon_Q \in [0.06...0.17]$ . Mass is  $m = 2.08$  kg.

Changes of resonance frequency  $f_0$  and transfer ratio at resonance  $\eta_0 = a_{sin}/A_{sin}$  (here,  $A_{sin}$  and  $a_{sin}$  are input and output vibration acceleration for sine vibration) controlled periodically during the test by sine vibration. If one of these parameters was deviate >20% of its initial value, vibration isolator is considered as disabled. Amplitude of sine vibration was  $A_{sin} = 10...30$  m/sec<sup>2</sup>.

Process of wearing is significantly depending of wire diameter. At Fig. 2, sleeves which parameters are out of 20% limit are shown.

Left sleeve made of wire  $d_w = 0.2$  mm is completely broken. Middle sleeve made of wire  $d_w = 0.15$  mm has many black dust (of worn-out wire) and broken pieces of wire. Right sleeve made of wire  $d_w = 0.1$  mm only changed its initial height and has very few dust. Its parameters are out of 20% limit, however if this limit will be wider, it is able to work at least twice more.

It is possible to explain this difference that for the same density MR material made of wire which diameter is little has more contact points. Wires of little diameter are more flexible. Wires of large diameter are not so flexible, stress in a few contact points is more and wires cut each other much more quickly.

Usually wearing leads to decreasing of resonance frequency. Wires cut each other, stiffness of vibration isolator decreases. Transfer ratio at resonance changes

insignificantly for little wire diameter ( $d_w = 0.1$  mm), little static deformation ( $\epsilon_Q = 0.06$ ) and little relative density ( $\bar{\rho} = 0.2$ ). For large wire diameter ( $d_w = 0.15...0.2$  mm) transfer ratio at resonance hardly decreases for large static deformation ( $\epsilon_Q = 0.12...0.17$ ) transfer ratio at resonance hardly increases. For large relative density ( $\bar{\rho} = 0.289$ ) resonance frequency during life-time is almost stabile, however transfer ratio at resonance hardly increases. If relative density ( $\bar{\rho} = 0.236$ ) is less this effect is less too (frequency decreases, transfer ratio at resonance slightly decreases). It means a different type of wearing for different parameters of MR material.

A stress was chosen as a load parameter for life-time research. Advantage of this parameter for load is that is includes load of random vibration (spectral density), mass load and size of vibration isolator. It is well-known an equation for calculation of middle value of acceleration under random load (Biderman, 1980):

$$a = \sqrt{\frac{\pi A f_0 \eta_0}{2}} \quad (1)$$

Here,  $A$  is spectral density of random load [(m/sec<sup>2</sup>)/Hz] is resonance frequency of system,  $\eta_0$  is transfer ratio on resonance. Thus, middle value of dynamic stress for random load in vibration isolator is:

$$\sigma_A = \frac{ma}{S} = \frac{m}{S} \sqrt{\frac{\pi A f_0 \eta_0}{2}} \quad (2)$$

Here:

$m$  = Mass of system

$S$  = Area of vibration isolator section

Vibration isolator has static preload too. Static stress in vibration isolator is (Ulanov, 2014):

$$\sigma_Q \approx (0.61 + 1.77\epsilon_Q - 20.4\epsilon_Q^2 + 160\epsilon_Q^3)\epsilon_Q \left( \frac{\bar{\rho}}{0.18} \right)^{1.7} \quad (3)$$

$$(-47.1d_w^2 + 16.5d_w - 0.174)$$

Common stress in vibration isolator is:

$$\sigma = \sigma_A + \sigma_Q \quad (4)$$

Life-time of vibration isolator depends on middle value of its deformation  $x$ , however, it depends on middle value of random acceleration  $a$ :

$$x = \frac{a}{4\pi^2 f_0^2} \quad (5)$$

Thus, dynamic stress includes the amplitude of vibration isolator deformation too. The dependency of life-time on frequency range of random load in the present experiments didn't find out.

Results of experiments are given in Fig. 3-5. Life-time  $T$  is in minutes. Equations of lines for dependency of life-time on wire diameter are:

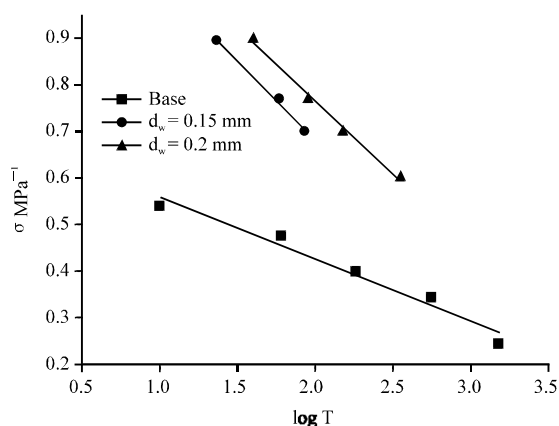


Fig. 3: Dependency of life-time on wire diameter;  $\bar{p} = 0.2$ ,  $\epsilon_Q = 0.06$ ; squares: base line ( $d_w = 0.1$  mm), circles:  $d_w = 0.15$  mm, triangles:  $d_w = 0.2$  mm

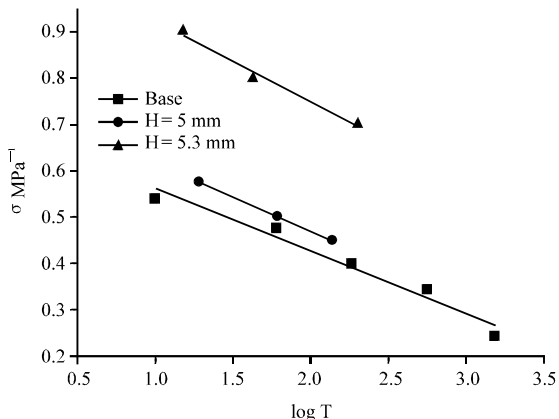


Fig. 4: Dependency of life-time on static deformation;  $\bar{p} = 0.2$ ,  $d_w = 0.1$  mm. Squares: base line ( $\epsilon_Q = 0.06$ ), circles:  $\epsilon_Q = 0.12$ , triangles:  $\epsilon_Q = 0.17$

- $\sigma = 0.69 - 0.13 \log T$  (for  $d_w = 0.1$  mm)
- $\sigma = 1.37 - 0.35 \log T$  (for  $d_w = 0.15$  mm)
- $\sigma = 1.40 - 0.32 \log T$  (for  $d_w = 0.2$  mm)

To obtain common equation for this lines one can divide coefficients of second and third equations by the same coefficients of first base equations. If first relative coefficient is  $\alpha_1$  and second one is  $\alpha_2$  result will be presented in a Table 1.

It is possible to describe the dependency of these coefficients on  $d_w$  by equations:

$$\alpha_1(d_w) = -3.78 + 66.6d_w - 188d_w^2 \quad (6)$$

$$\alpha_2(d_w) = -7.54 + 121.6d_w - 350d_w^2 \quad (7)$$

Thus, common equation will be  $\sigma = 0.69\alpha_1(d_w) - 0.13\alpha_2(d_w)\log T$ . Equations of lines for dependency of life-time on static deformation are:

- $\sigma = 0.69 - 0.13 \log T$  (for  $\epsilon_Q = 0.06$ )
- $\sigma = 0.76 - 0.15 \log T$  (for  $\epsilon_Q = 0.12$ )
- $\sigma = 1.10 - 0.18 \log T$  (for  $\epsilon_Q = 0.17$ )

Relative coefficients are presented in a Table 2. It is possible to describe the dependency of these coefficients on  $\epsilon_Q$  by equations:

$$\alpha_1(\epsilon_Q) = 1.43 - 11.94\epsilon_Q + 73.9\epsilon_Q^2 \quad (8)$$

Table 1: Relative coefficients for wire diameter

$d_w$	$\alpha_1$	$\alpha_2$
0.1	1.00	1.00
0.15	1.99	2.69
0.2	2.02	2.46

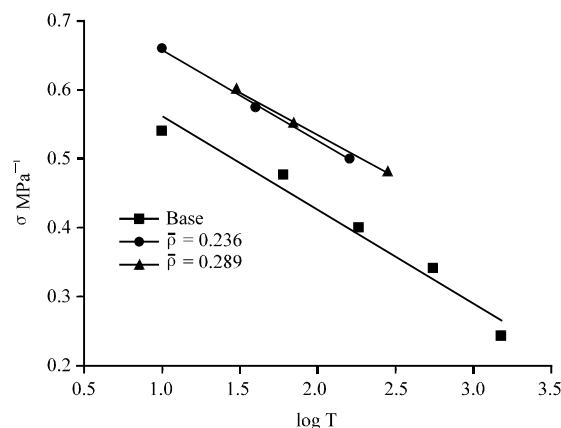


Fig. 5: Dependency of life-time on relative density;  $d_w = 0.1$  mm,  $\epsilon_Q = 0.06$ ; squares: base line ( $\bar{p} = 0.2$ ); circles:  $\bar{p} = 0.236$  and triangles:  $\bar{p} = 0.289$

Table 2: Relative coefficients for static deformation

$\varepsilon_Q$	$\alpha_1$	$\alpha_2$
0.06	1.00	1.00
0.12	1.10	1.15
0.17	1.59	1.38

Table 3: Relative coefficients for relative density

$\bar{\rho}$	$\alpha_1$	$\alpha_2$
0.2	1.00	1.00
0.236	1.14	0.98
0.289	1.12	0.91

$$\alpha_2(\varepsilon_Q) = 0.99 - 0.94\varepsilon_Q + 19.1\varepsilon_Q^2 \quad (9)$$

Thus, common equation will be  $\sigma = 0.69\alpha_1(\varepsilon_Q) - 0.13\alpha_2(\varepsilon_Q) \log T$ . Equations of lines for dependency of life-time on relative density are:

- $\sigma = 0.69 - 0.13 \log T$  (for  $\bar{\rho} = 0.2$ )
- $\sigma = 0.79 - 0.135 \log T$  (for  $\bar{\rho} = 0.236$ )
- $\sigma = 0.78 - 0.12 \log T$  (for  $\bar{\rho} = 0.289$ )

Relative coefficients are presented in a Table 3. It is possible to describe the dependency of these coefficients on  $\varepsilon_Q$  by equations:

$$\alpha_1(\bar{\rho}) = -2.04 + 24.8\bar{\rho} - 47.9\bar{\rho}^2 \quad (10)$$

$$\alpha_2(\bar{\rho}) = 0.71 + 3.19\bar{\rho} - 8.60\bar{\rho}^2 \quad (11)$$

Thus common equation will be  $\sigma = 0.69\alpha_1(\bar{\rho}) - 0.13\alpha_2(\bar{\rho}) \log T$ . Common equation of all lines is:

$$\sigma = 0.69\alpha_1(d_w)\alpha_1(\varepsilon_Q)\alpha_1(\bar{\rho}) - 0.13\alpha_2(d_w)\alpha_2(\varepsilon_Q)\alpha_2(\bar{\rho}) \log T$$

Thus, equation for life-time calculation is:

$$T = 10^{\frac{0.69\alpha_1(d_w)\alpha_1(\varepsilon_Q)\alpha_1(\bar{\rho}) - \sigma}{0.13\alpha_2(d_w)\alpha_2(\varepsilon_Q)\alpha_2(\bar{\rho})}} \quad (12)$$

where coefficients are from Eq. 6-11, stress is from Eq. 2-4 and life-time is in minutes. Dependencies of life-time on  $d_w$ ,  $\varepsilon_Q$  and  $\bar{\rho}$  are approximately linear in the range of experiment. However, it is impossible that all these lines cross any coordinate axis (it would mean negative stress or life-time). It means that out of the range of experiment these dependencies have non-linear parts, approach to the axis. Left parts of these dependencies are not interesting for practical use, because life-time for them is  $>10$  min. Right parts require very long experiment ( $>2000$  min). This problem needs future research.

## CONCLUSION

Random load changes structure of MR material. It is enough only a few minutes of random load (2 min in the present experiments) for it. If MR has large preliminary static deformation, there is large stress in wire contacts. Random load disturbs these contacts, some of them slip, and stiffness of MR reduces. Resonance frequency of vibration isolator becomes less. For relative static deformation  $<0.12$  this effect is insignificant ( $<4\%$ ) if relative static deformation is 0.17, initial resonance frequency reduces about 16% (for  $d_w = 0.1$  mm). Large wire diameter (0.15...0.2 mm) reduces this effect approximately twice (to 8%), influence of relative density didn't find out. Random load changes a friction in MR material too. Transfer ratio at resonance after 2 min under random vibration becomes less. For relative static deformation  $<0.12$  this effect is insignificant ( $<6\%$ ) if relative static deformation is 0.17, initial transfer ratio at resonance reduces about 33% (for  $d_w = 0.1$  mm). Large wire diameter (0.15...0.2 mm) reduces this effect approximately twice (to 17%), influence of relative density didn't find out too. This changing of structure should depend on a level of random load, thus this question needs future research too. It is necessary to take into account these effects for calculation of vibration protection system under random load.

There are other damping wire materials beside MR for example "Spring Cushion" manufactured by Stop-Choc Company (Germany). Comparison of vibration insulators made of this material and MR material is presented by Lazutkin *et al.* (2014). Problem of life-time is important for all types of pressed wire vibration insulators. Thus, it is possible to use a method developed in the present study for obtaining its life-time characteristics under random load too.

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